



Cohesive Laws for Adhesive Tapes

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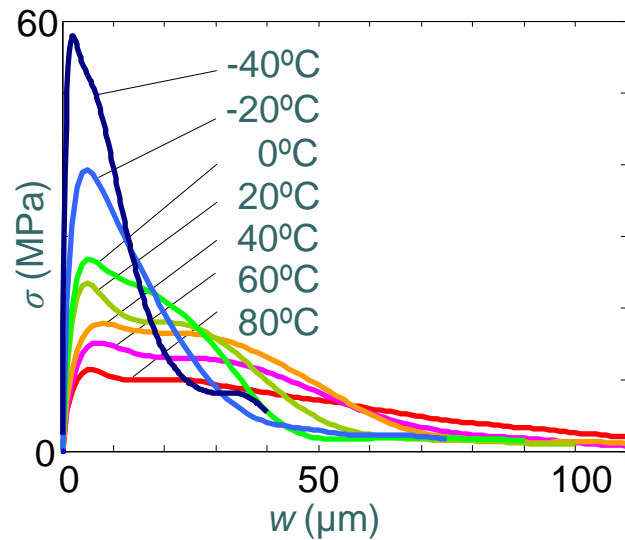
Technical University of Denmark
Department of Wind Energy
Denmark

Introduction

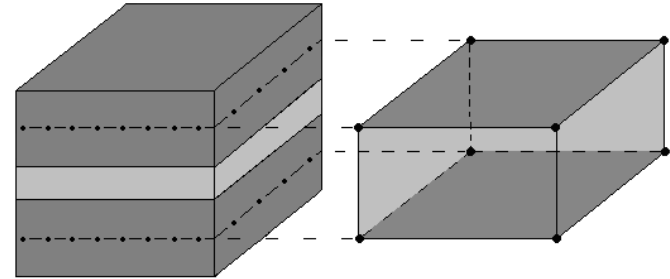
1) Experiment



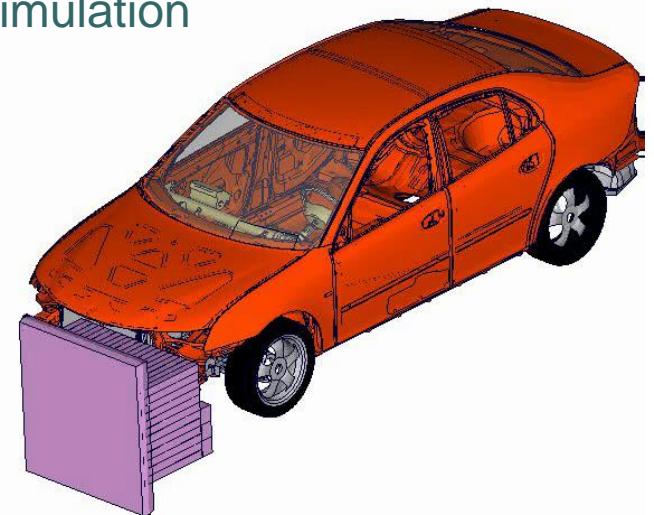
2) Cohesive laws



3) FE-element

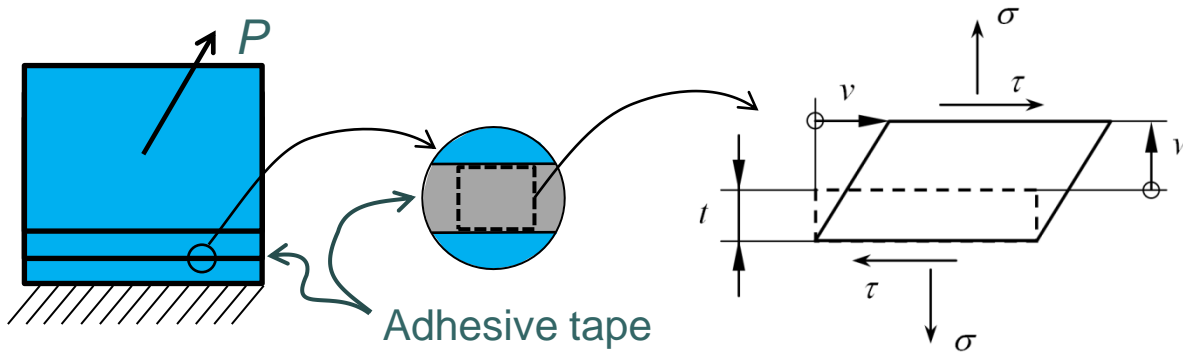


4) Simulation



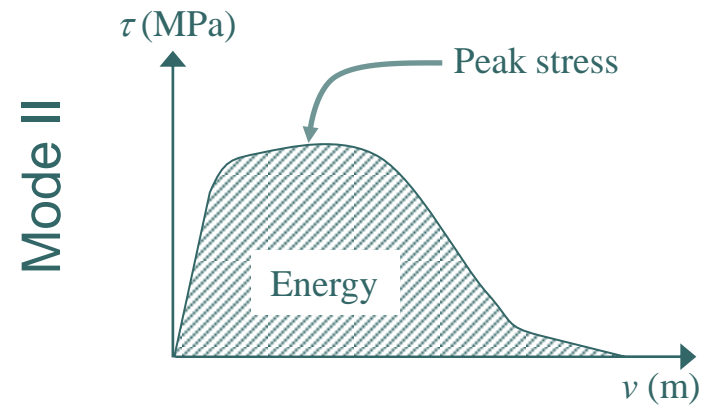
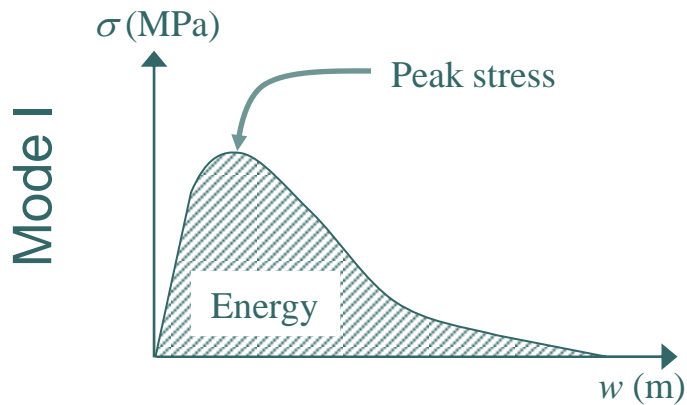
Cohesive law

Layer (adhesive tape) exposed to a load – two kind of deformations



Mode I $\rightarrow \sigma$
 Mode II $\rightarrow \tau$
 Mixed mode $\rightarrow \tau$ and σ

Cohesive law

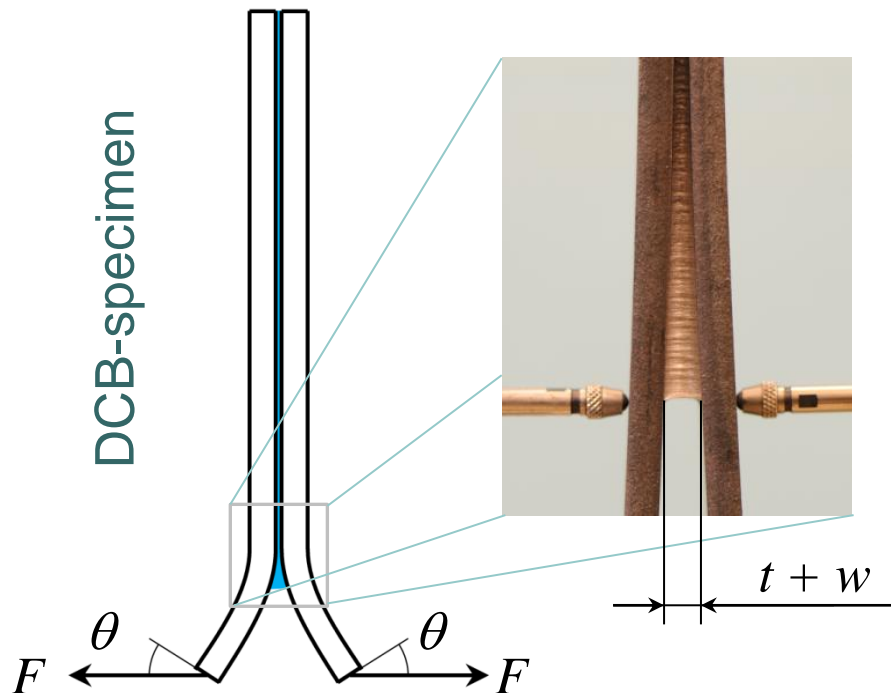


Experimental method

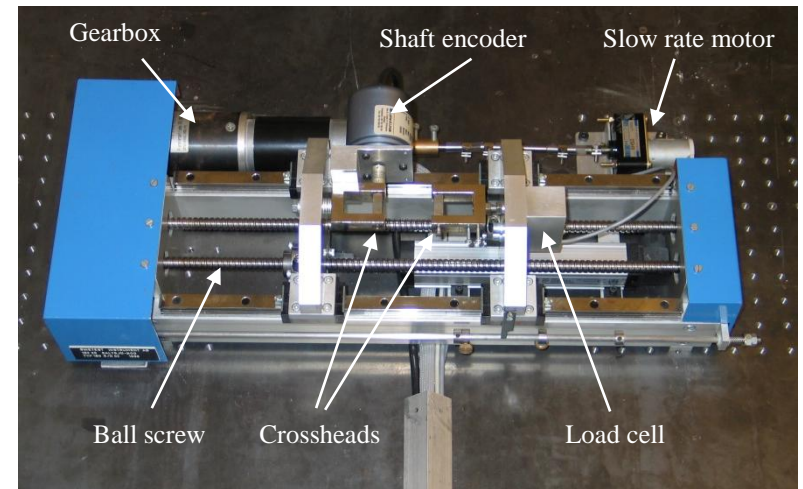
$$J = \frac{2F \sin \theta}{b}$$

$$J = \int \sigma dw$$

$$\sigma = \frac{dJ}{dw} = \frac{d}{dw} \left(\frac{2F \sin \theta}{b} \right)$$



Tensile test machine



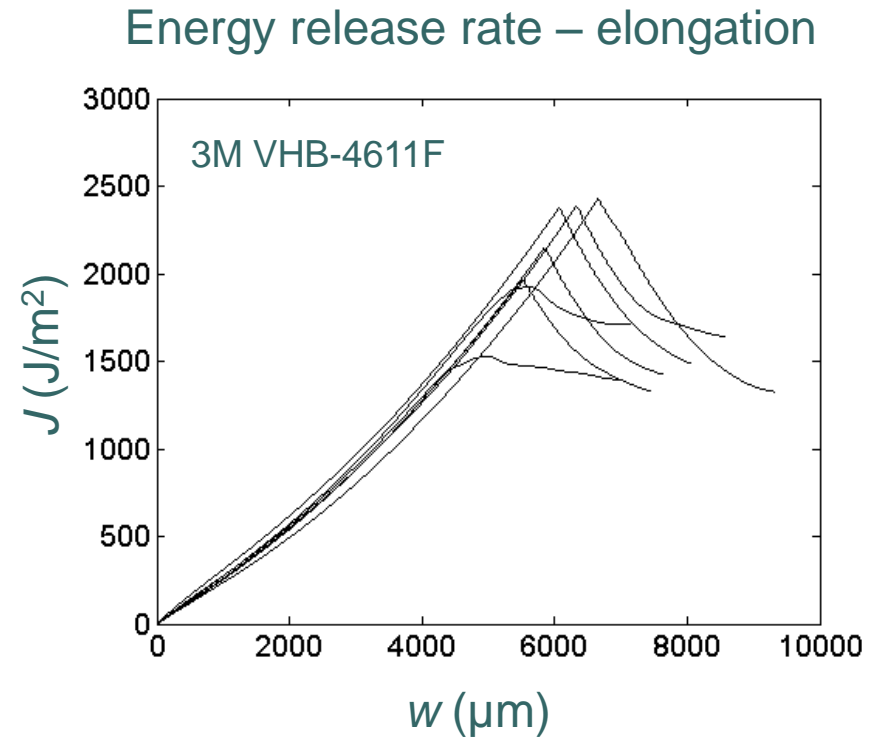
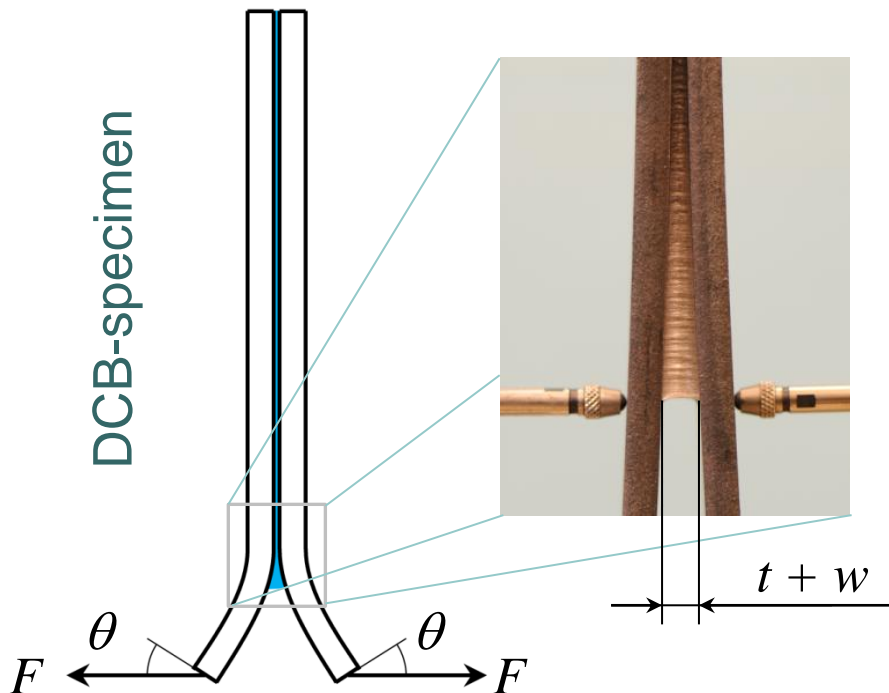
- The elongation, w at the start of the adhesive layer is measured with two LVDTs
- The rotation is measured with a shaft encoder
- Constant loading rate

Mode I, Energy Release Rate

$$J = \frac{2F \sin \theta}{b}$$

$$J = \int \sigma dw$$

$$\sigma = \frac{dJ}{dw} = \frac{d}{dw} \left(\frac{2F \sin \theta}{b} \right)$$



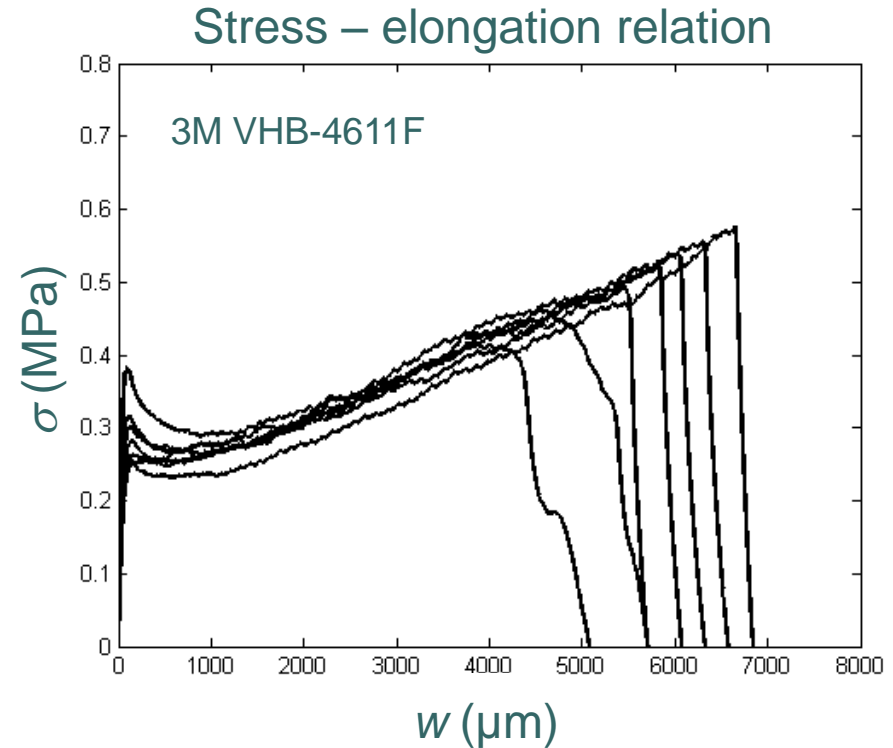
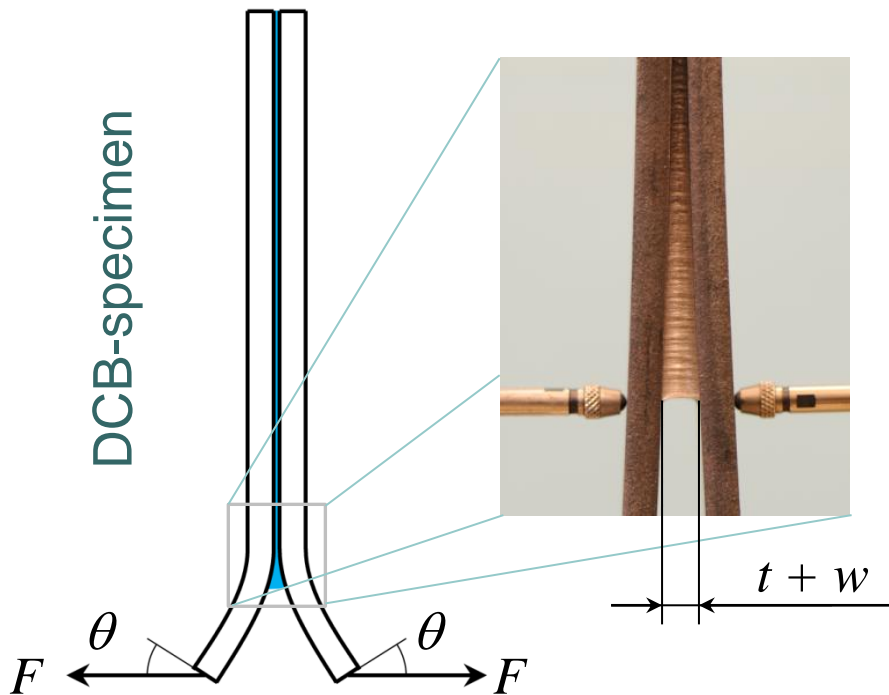
Constant loading rate 30 $\mu\text{m}/\text{s}$

Mode I, Cohesive Law

$$J = \frac{2F \sin \theta}{b}$$

$$J = \int \sigma dw$$

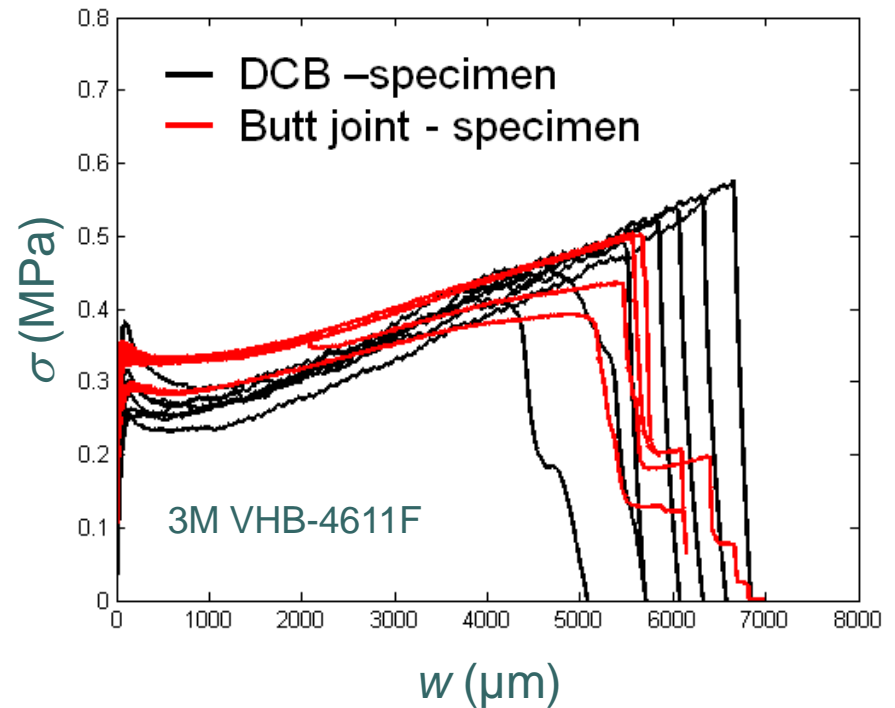
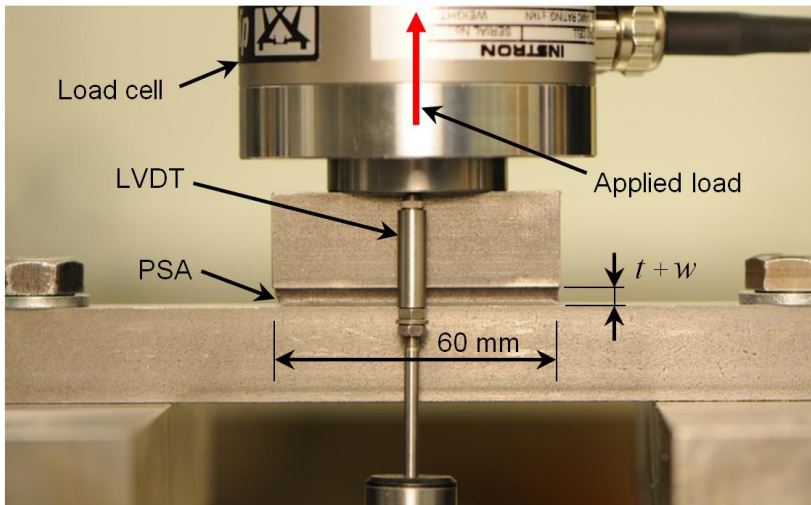
$$\sigma = \frac{dJ}{dw} = \frac{d}{dw} \left(\frac{2F \sin \theta}{b} \right)$$



Butt-joint

$$\sigma = \frac{F}{A}$$

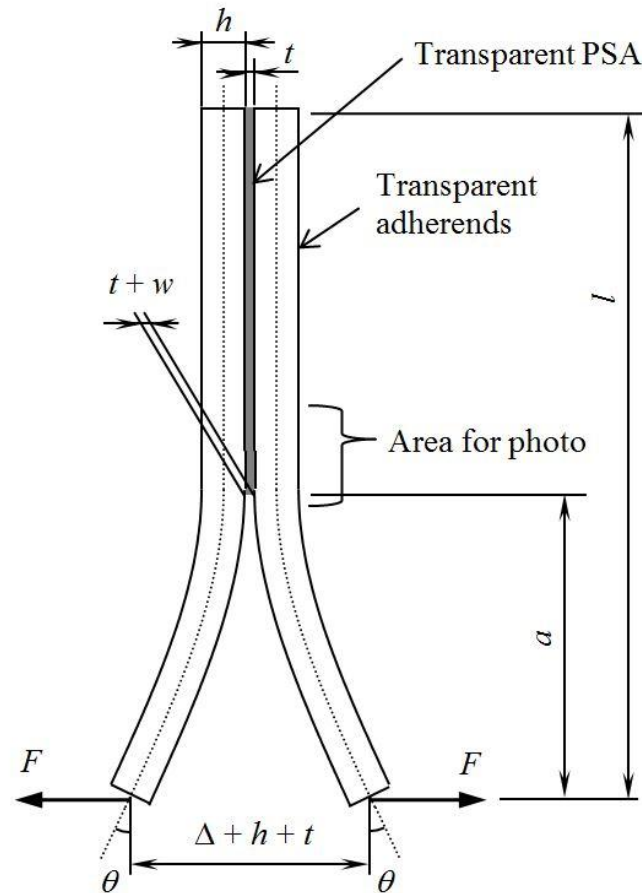
Stress – elongation relation



- Constant loading rate 10 $\mu\text{m/s}$
- Similar result
- Two peak stresses



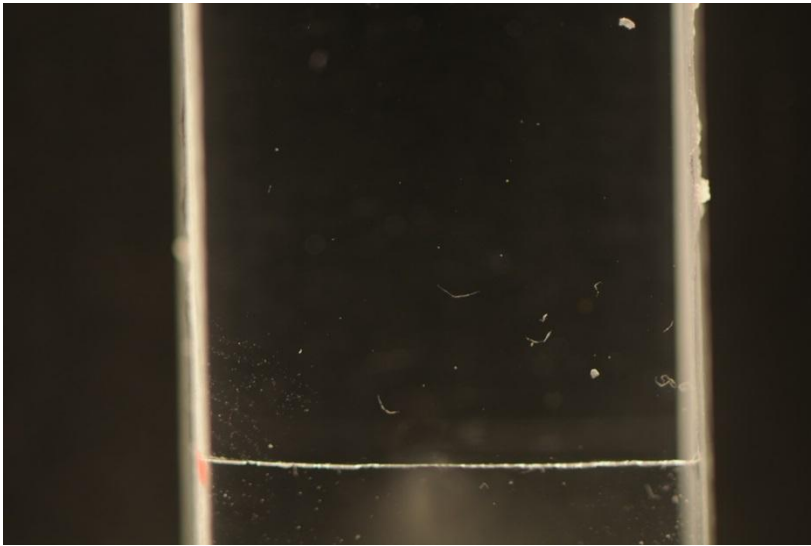
Mode I – Transparent



- Adherends made of *PMMA*
- Transparent tape (3M-4905F)
- Enables the study of crack initiation and growth
- Crack growth is photographed during the experiment

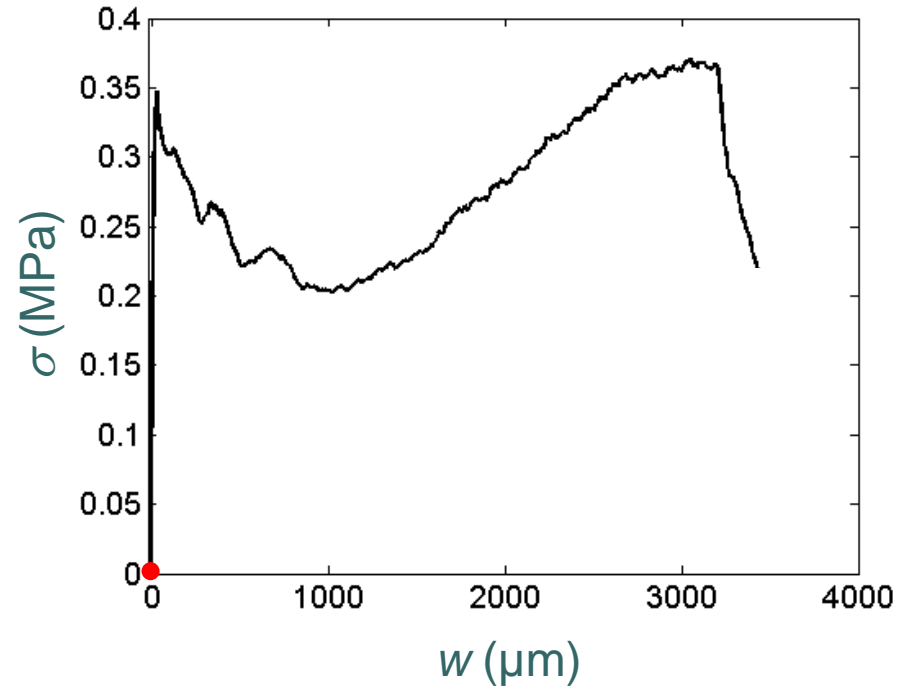
Mode I - PMMA

Fracture process



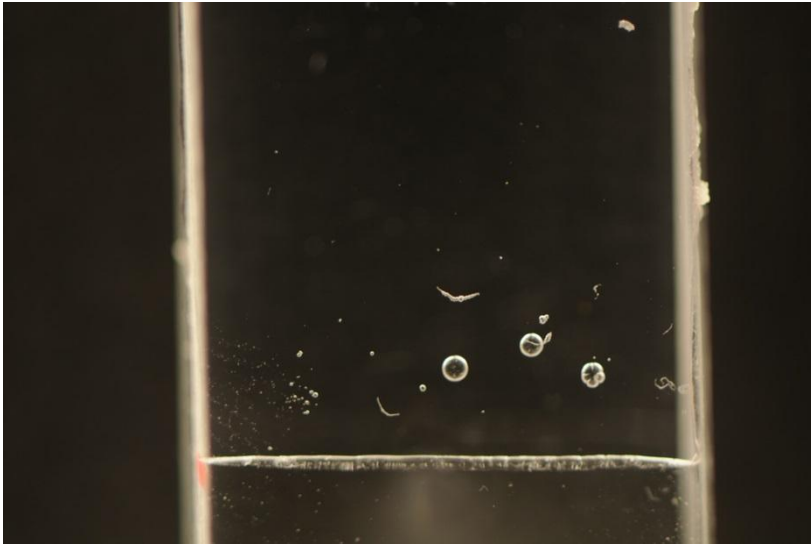
$w = 0 \mu\text{m}$

Stress – elongation relation



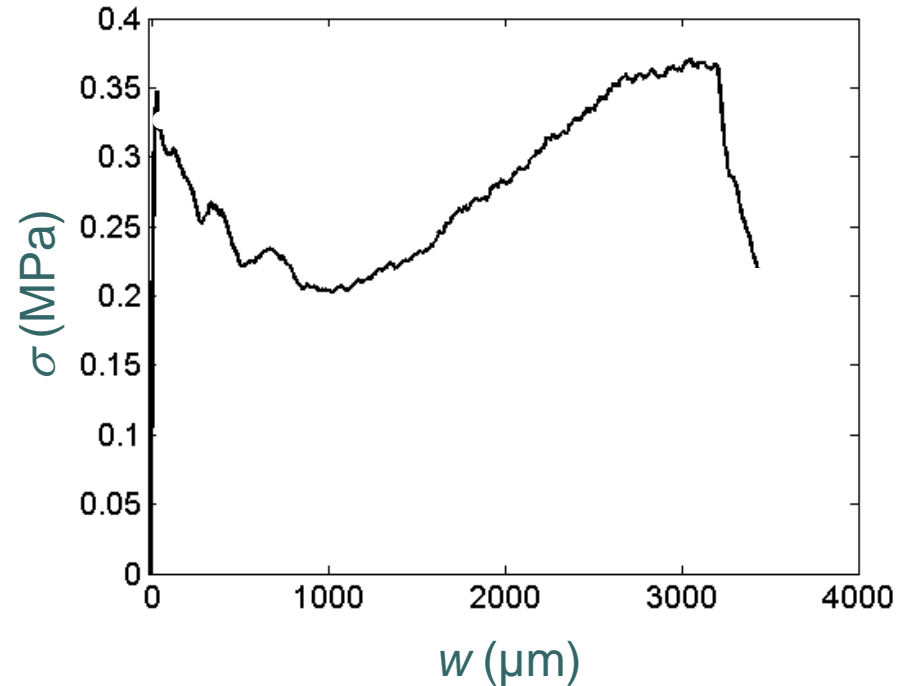
Mode I - PMMA

Fracture process



$w = 50 \mu\text{m}$

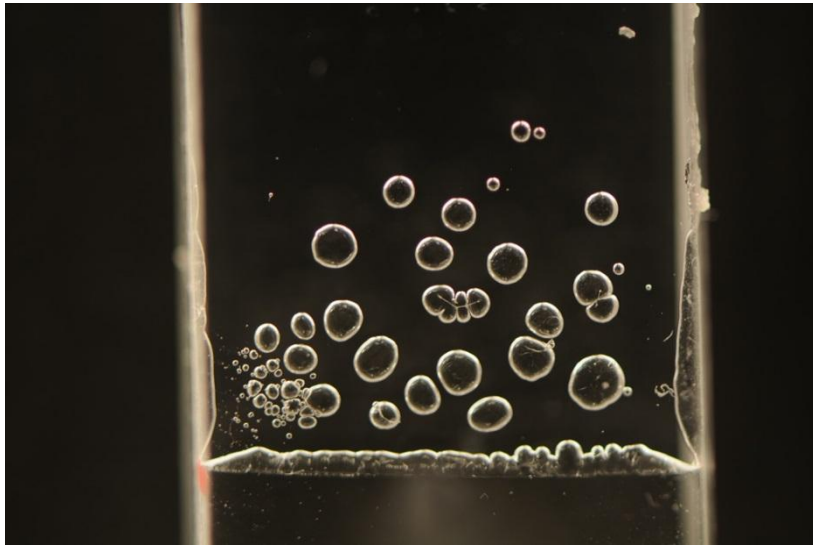
Stress – elongation relation



Creation of small cavities – stress starts to decrease

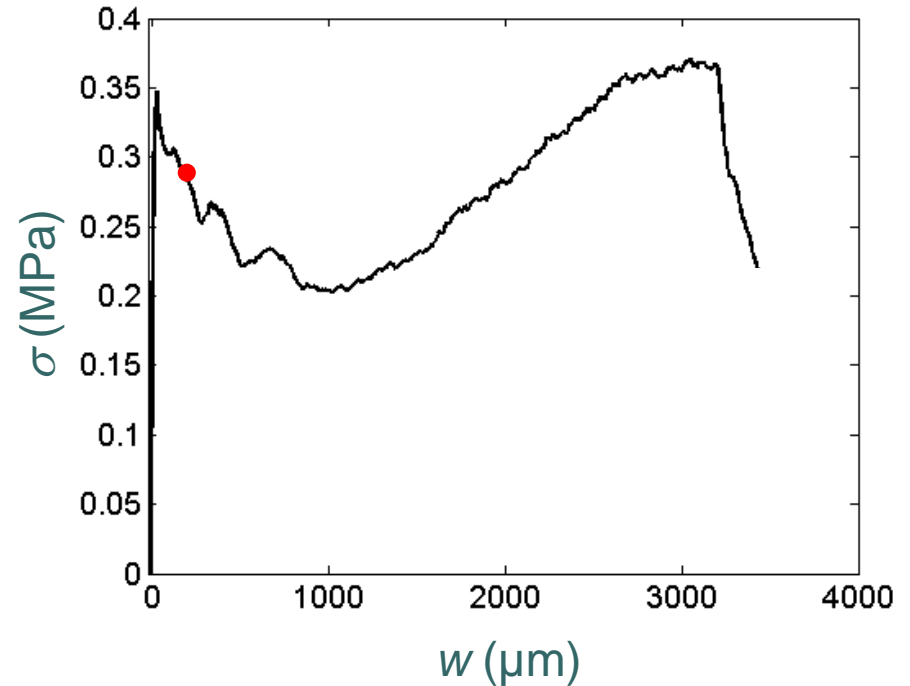
Mode I - PMMA

Fracture process



$w = 250 \mu\text{m}$

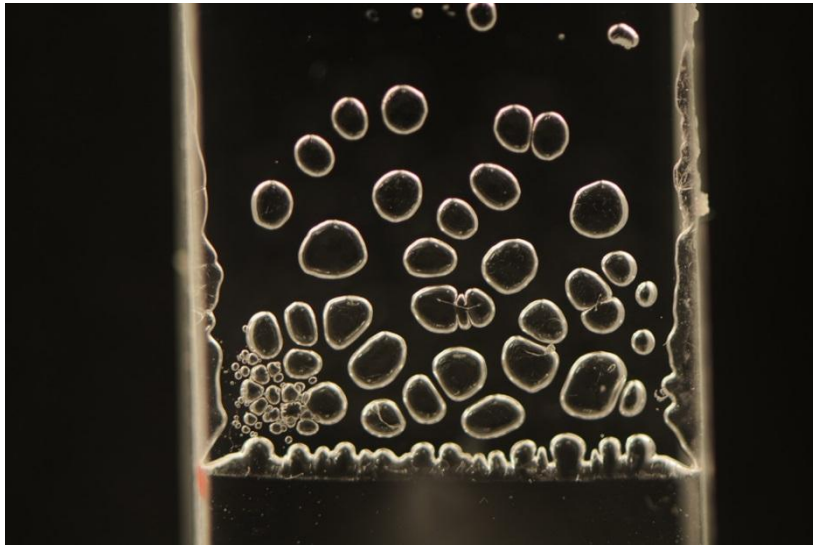
Stress – elongation relation



Number of and the size of the cavities is growing

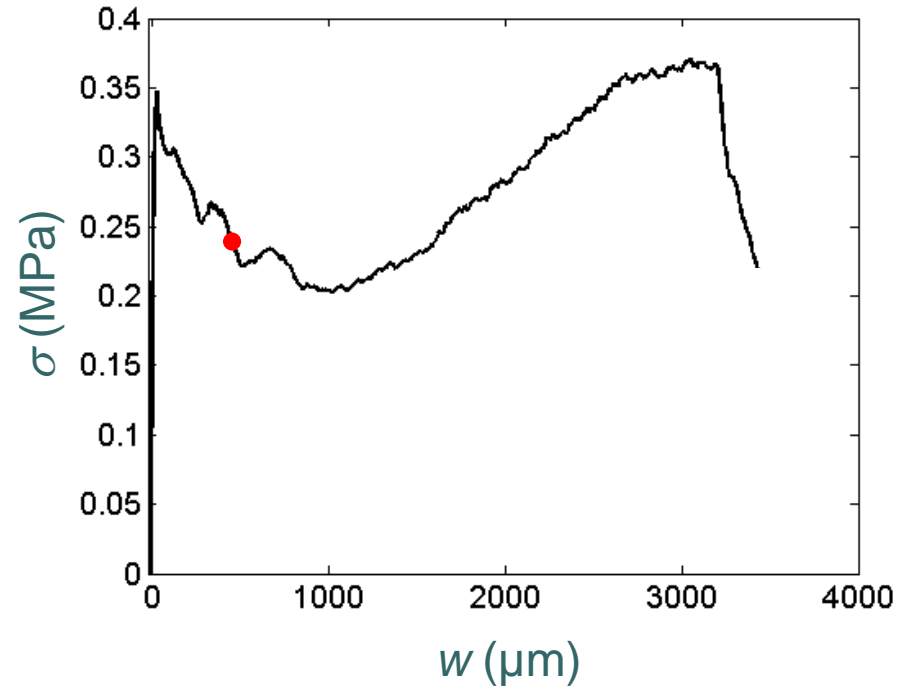
Mode I - PMMA

Fracture process



$w = 500 \mu\text{m}$

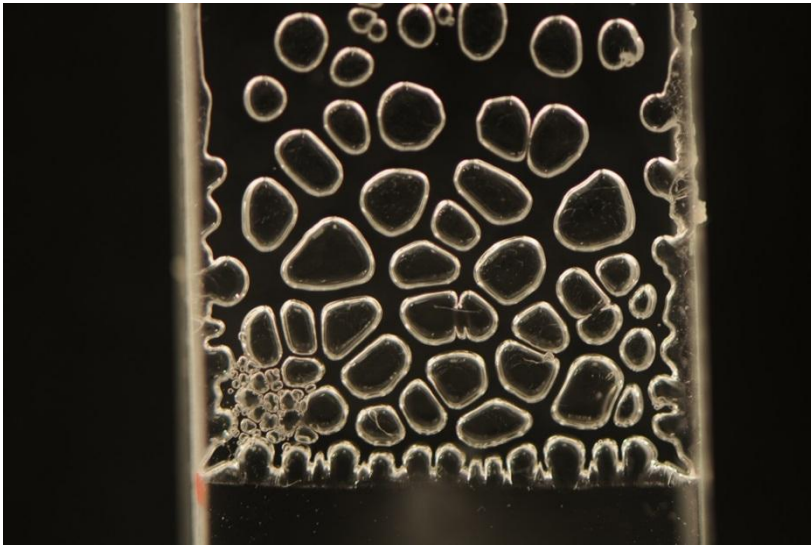
Stress – elongation relation



Number of and the size of the cavities is growing

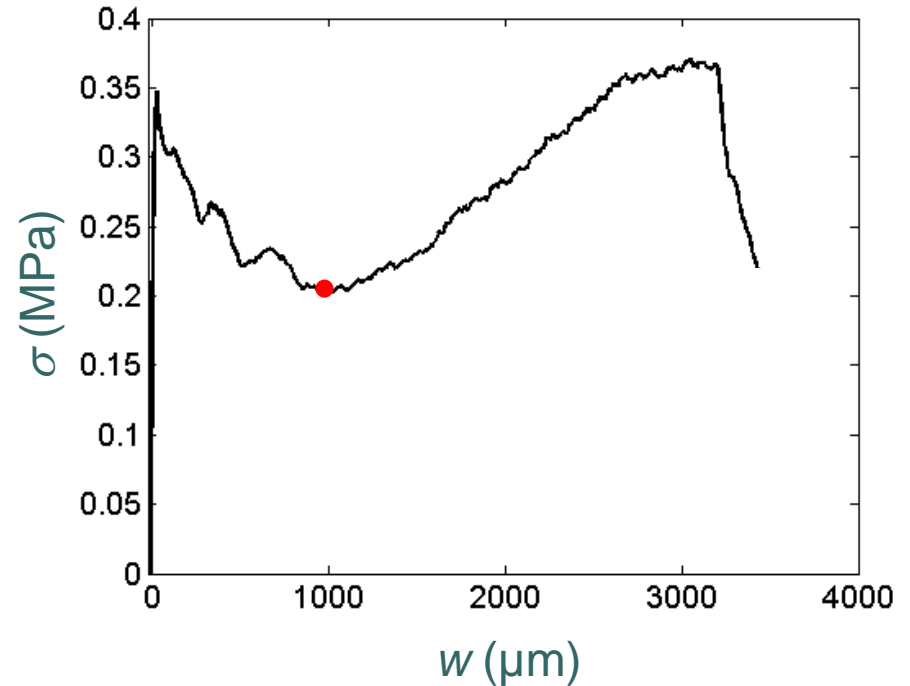
Mode I - PMMA

Fracture process



$w = 1000 \mu\text{m}$

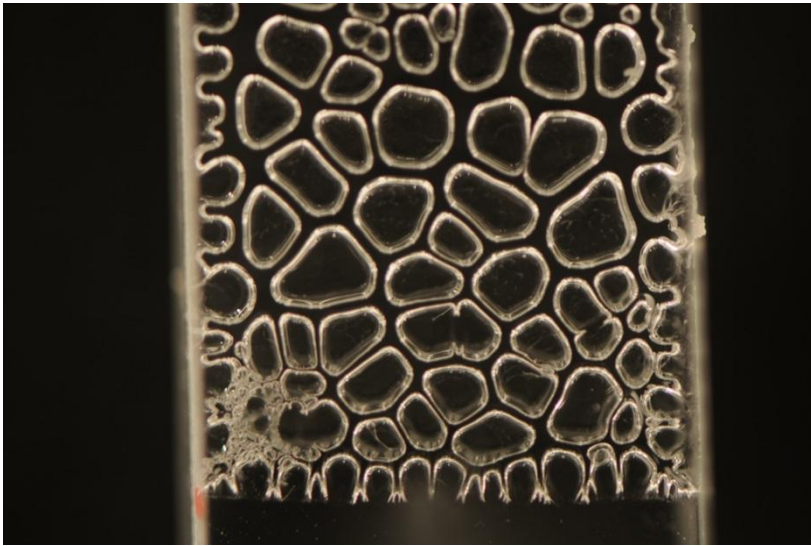
Stress – elongation relation



Cavities is covering the entire width of the specimen

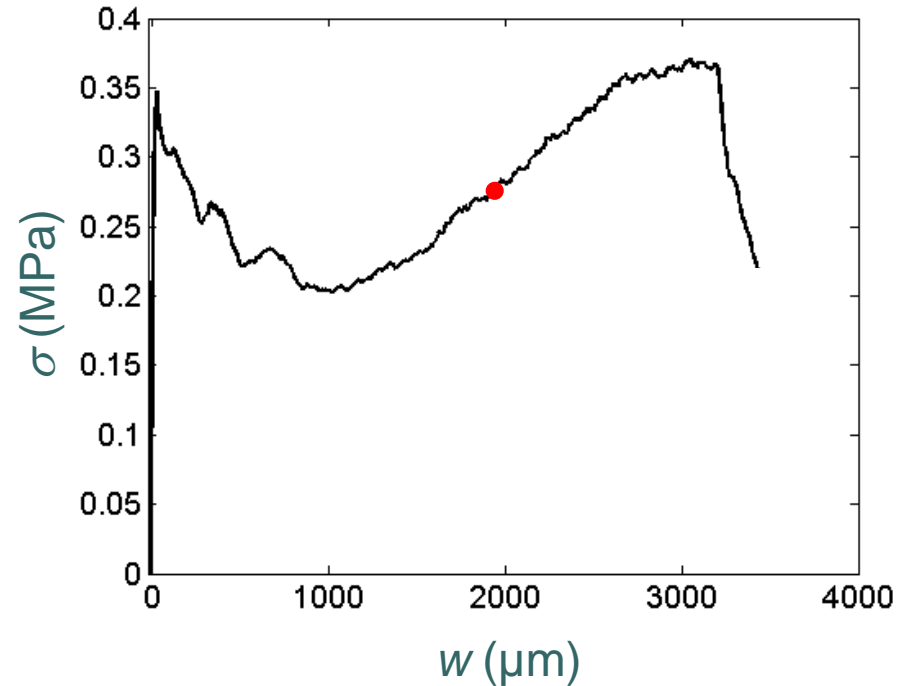
Mode I - PMMA

Fracture process



$w = 2000 \mu\text{m}$

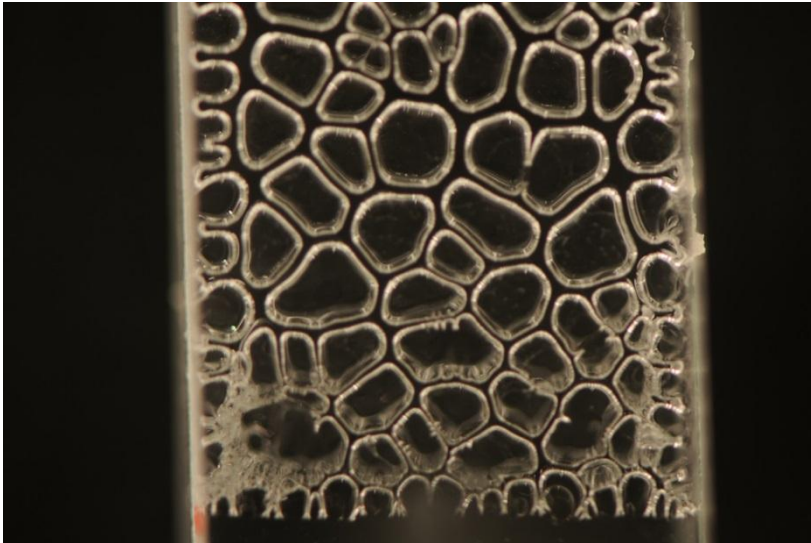
Stress – elongation relation



The growth of the cavities is limited - The stress is increasing

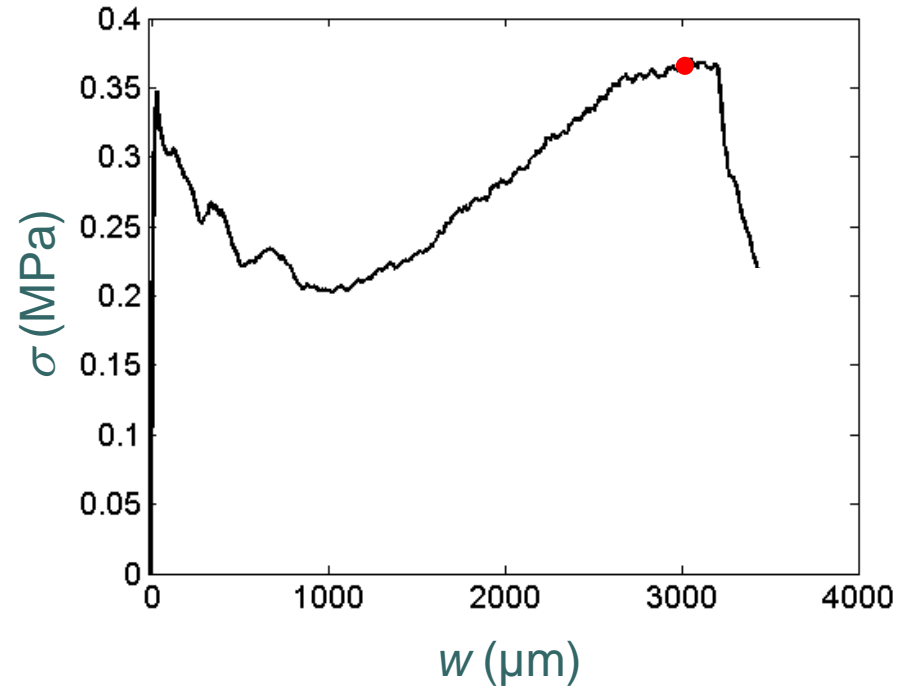
Mode I - PMMA

Fracture process



$w = 3000 \mu\text{m}$

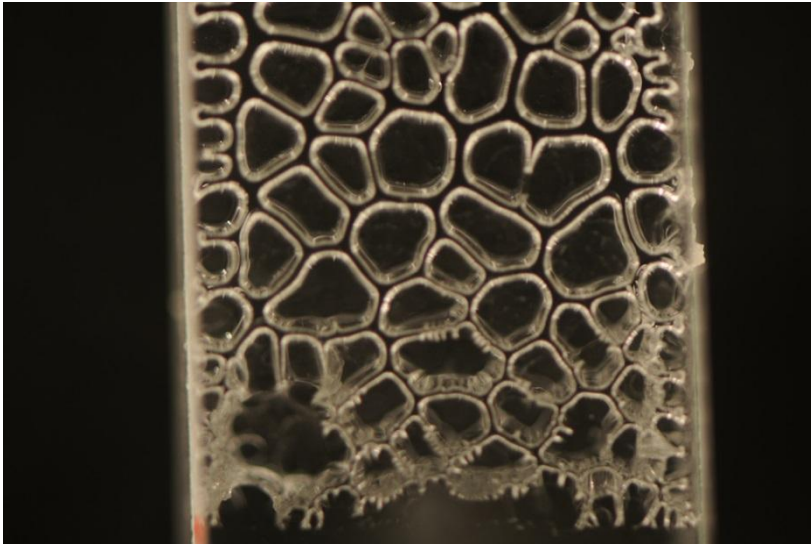
Stress – elongation relation



Cavities start to grow together

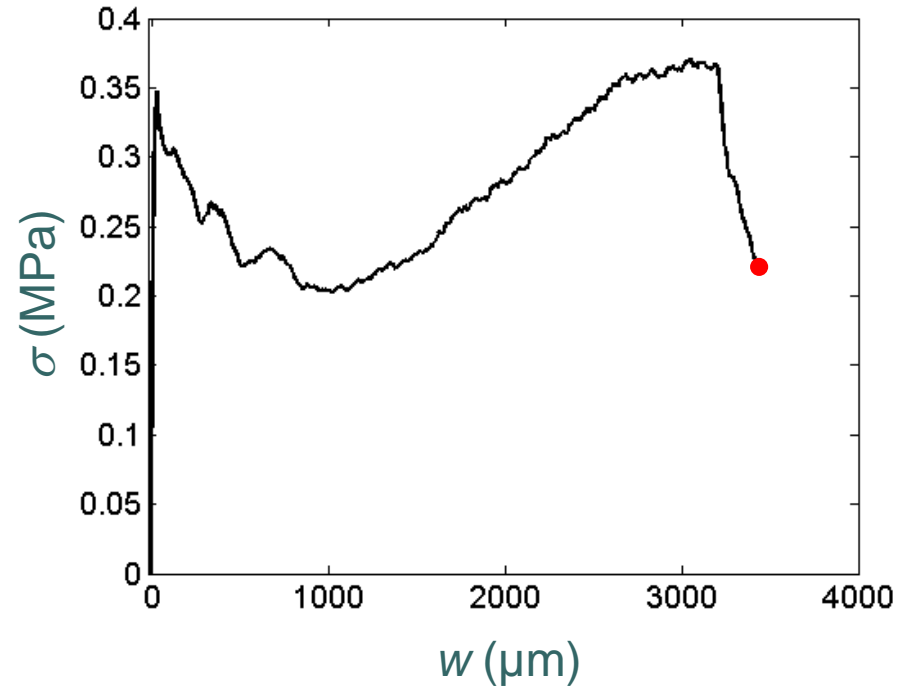
Mode I - PMMA

Fracture process



$w = 3500 \mu\text{m}$

Stress – elongation relation



Macroscopic crack is created

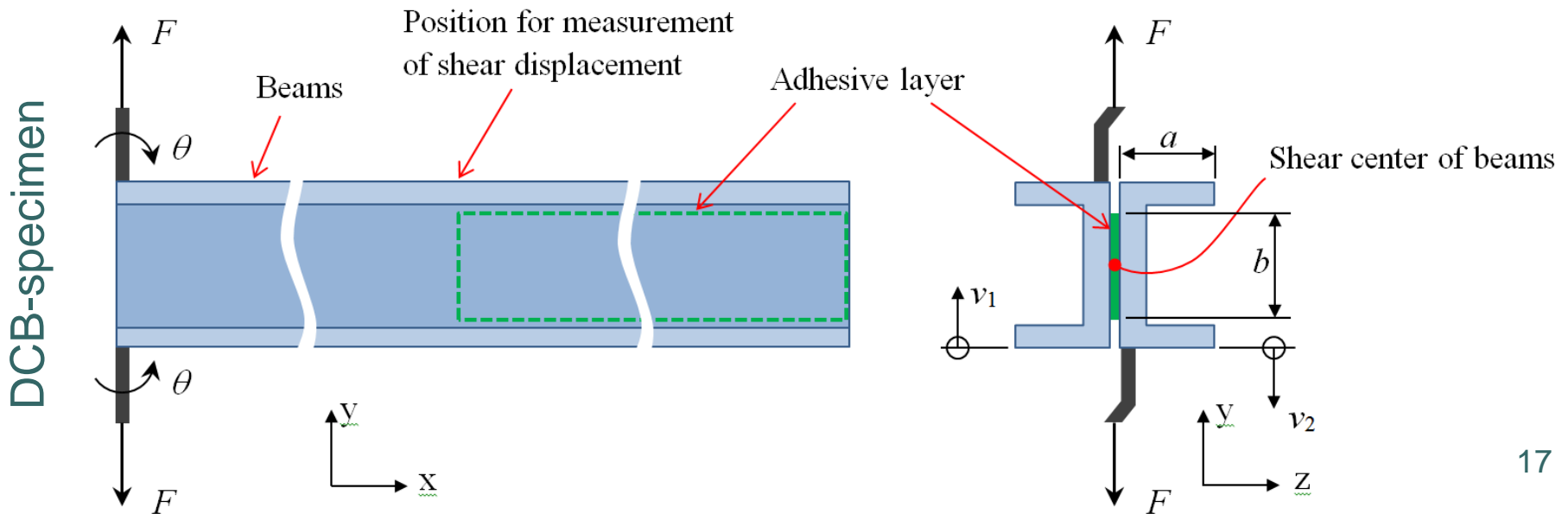
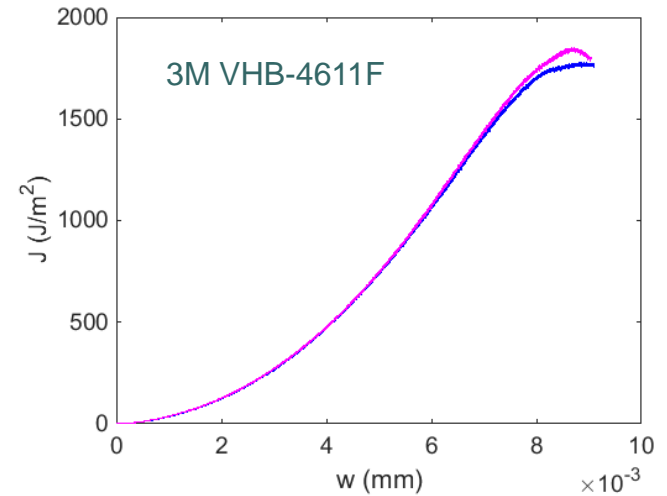
Mode II, Energy Release Rate

$$J = \frac{2F \sin \theta}{b}$$

$$J = \int \sigma dw$$

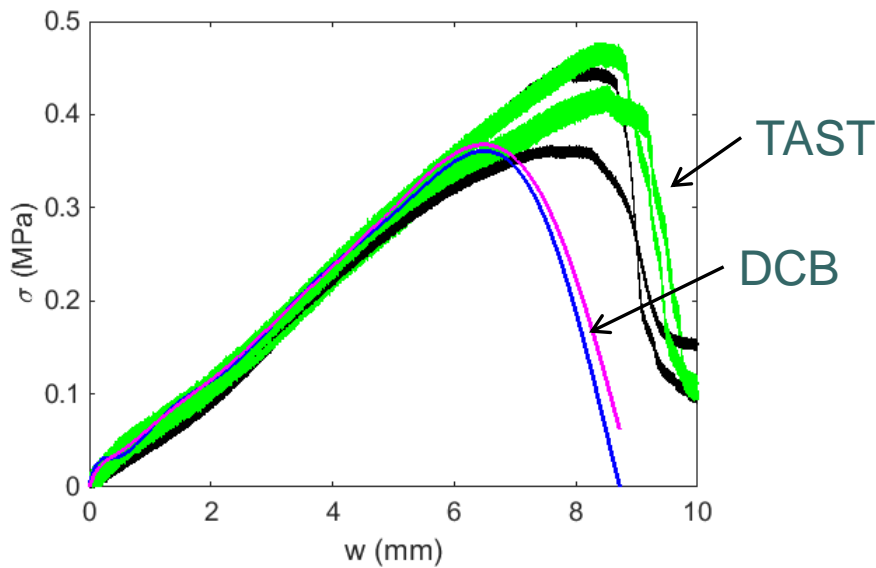
$$\sigma = \frac{dJ}{dw} = \frac{d}{dw} \left(\frac{2F \sin \theta}{b} \right)$$

$$w = v_1 - v_2$$

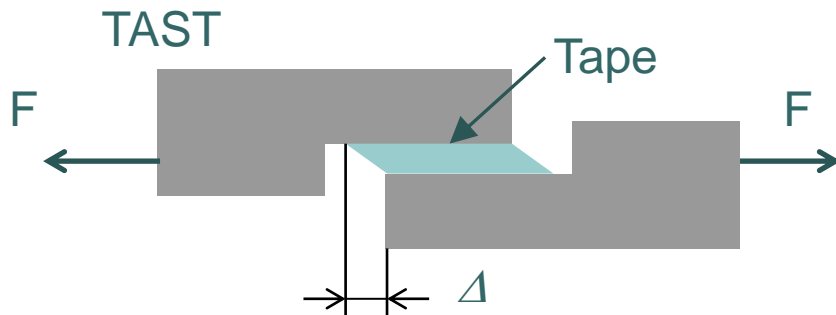
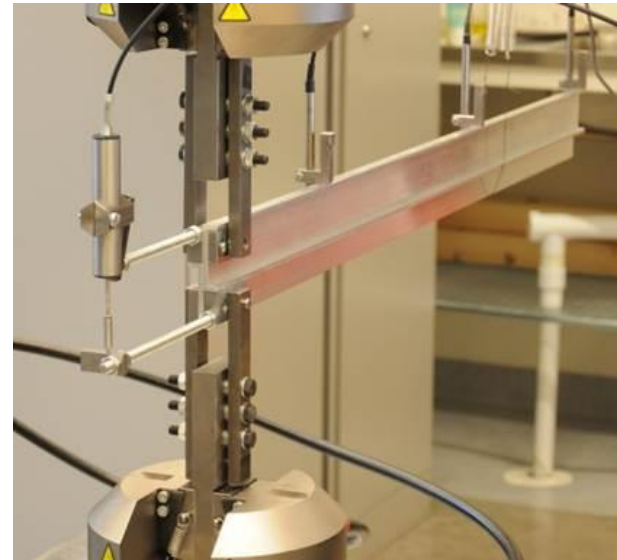


Mode II, Cohesive Law

Cohesive law



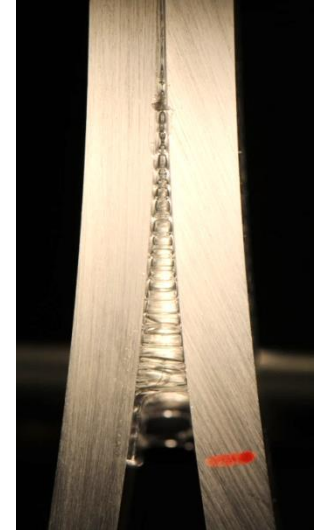
DCB experiment for shear



Behaviour for shear is not influenced by cavities

Result and Conclusions

- Adhesive tapes has a low maximum stress but an impressive fracture energy
- Similar result is obtained by use of different methods/geometries
DCB-specimen – Butt joint - TAST
- The cohesive law for *Mode I* is influenced by the creation, growth and coalescence of cavities
- The cohesive law for *Mode II* is almost bi-linear.



3M VHB-4611F	Mode I	Mode II
Fracture energy	2100 J/m ²	2000 J/m ²
Peak stress	0.5 MPa	0.4 MPa

